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Integer representations

We have a byte, which consists of 8 bits. What integers can be represented using a byte? The answer depends on how we interpret the bits. With 8 bits, we have $(2^8 = 256)$ different possible combinations, so 256 different values can be stored.

For example, one everyday use of these 8 bits is to represent <u>unsigned integers</u> in the range [0..255]. These numbers are all *non-negative*; this data type is typically referred to as a byte or an <u>unsigned short int</u> in many programming languages.

Example: how to add two binary numbers?

But what happens if we need to store negative numbers as well? How can we represent both positive and negative integers?

One common solution is reserving the *highest-order bit* (the most significant bit, also known as the 7th bit, since counting starts from zero) as a sign bit. This bit indicates the sign of the number, and it is often denoted as the sign bit, 's'.

- If the sign bit (s) is 0, the number is positive or zero.
- If the sign bit (s) is 1, the number is negative.

The remaining **7 bits** are used to represent the magnitude of the number, either positive or negative. This method allows us to represent integers in the range [-128..+127]. In other words:

- If the sign bit is 0, the number is in the range [0 .. 127].
- If the sign bit is 1, the number is in the range [-1 .. -128].

This is a simple form of sign-magnitude representation.

Two's Complement Representation

In modern computing, <u>two's complement</u> is a more commonly used method for representing signed integers. In this system, the highest-order bit is also used as the sign bit, but the way negative numbers are stored differs. Here's how it works:

- The most significant bit is still used as the sign bit, where 0 indicates a positive number, and 1 indicates a negative number.
- However, negative numbers are represented by taking the two's complement of their absolute value. This involves inverting all the bits and then adding 1 to the result.

Example: Encode -5 with two's complement method with 8 bits.

- The number 5 in binary (in an 8-bit system) is represented as 00000101
- Invert the bits: 11111010

• Add one: **11111011**

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