

Floating-Point Representation

Floating-point representation is used to store real numbers, especially when dealing with very large or very small values. It approximates real numbers in a way that balances precision and range.

The IEEE 754 Standard

The IEEE 754 standard is the most common way to represent floating-point numbers. It splits a floating-point number into three components:

- **Sign (S)**: Determines if the number is positive or negative (1 bit).
- **Exponent (E)**: Represents the number range (8 bits for single-precision).
- **Mantissa (M)** (also called the significant or fraction): Represents the precision (23 bits for single-precision).

The formula:

$$\text{Value} = (-1)^S \times 1.M \times 2^{(E - \text{Bias})}$$

where **Bias** is 127 for single-precision (32-bit).

Single-Precision (32-bit) Example

Let's break down the number **10.25** in binary to see how it's represented:

- **Step 1**: Convert **10.25** to binary:
 - Integer part: **10** in binary is **1010**.
 - Fraction part: **0.25** is **0.01** in binary.
 - So, **10.25** in binary is **1010.01**
- **Step 2**: Normalize it into scientific notation in binary:

$$1010.01 = 1.01001 \times 2^3$$

- **Step 3**: Identify the components:
 - **Sign (S)**: 0 (positive)
 - **Exponent (E)**: We add the bias (127) to the actual exponent (3), so **E = 3 + 127 = 130**. In binary: **1000010**
 - **Mantissa (M)**: We drop the leading 1 from **1.01001**, so the mantissa is 010010... (with trailing zeros to make 23 bits)
- **Step 4**: Combine them

$$0 \mid 1000010 \mid 01001000000000000000000$$

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